Probability-Answers

Key Stage3: 2003 Paper 1 Level 3-5

ier & Que			Throwing dice	
-5 4-6 5-	7 6-8			
0 5		Correct response	Additional guidance	
a a	2m	Indicates only the five points with positive integer coordinates whose sum is 6 eg	! Point(s) not indicated accurately Accept in parts (a) and (b) provided the pupil's intention is clear	
		* * * * * * * * * * * * * * * * * * * *	! Additional points indicated that assume zero to be on the dice eg • (0, 6) and/or (6, 0) indicated If this is the only error, mark as 1, 0 ! Additional points with non-integer coordinates whose sum is 6 indicated eg	
	or 1m	Indicates at least four correct points with no incorrect points or Indicates all five correct points with not more than one incorrect point	If this is the only error, mark as 1, 0	
b	2m	Indicates only the six points with positive integer coordinates such that $y = x$ eg	! Additional point indicated that assumes zero to be on the dice eg • (0, 0) indicated If this error has been penalised in part (a), condone If this is the only error and it has not been penalised in part (a), mark as 1, 0 ! Additional points with non-integer coordinates such that y = x indicated eg •	
	or 1m	Indicates at least five correct points with no incorrect points or Indicates all six correct points with not more than one incorrect point	If this error has been penalised in part (a), condone If this is the only error and it has not been penalised in part (a), mark as 1, 0	

Tier & Question					Thursday disa (sout)	
-5 4-	6 5-	6-8			Throwing dice (cont)	
0 5	1			Correct response	Additional guidance	
c c			1m	Completes the sentence to give a correct rule eg One less than the number on the red dice Red - 1 Needing 1 added to get the number on the red dice	✓ Minimally acceptable rule eg • 1 below the other dice • The number below the red dice	
					! Rule that does not use the given starting phrase Accept only if unambiguous eg, accept • Red = blue + 1 eg, do not accept • 1 more on the red	
					■ Ambiguous rule eg • − 1 • 1 below • A number below the red dice • The number lower than the red dice • Followed by the number on the red dice	
					x Incomplete rule eg • Less than the number on the red dice • The second se	
					 ➤ Rule not generalised Do not accept rules only shown through particular numerical examples eg • 2 - 1 = 1, 3 - 2 = 1, 4 - 3 = 1 etc 	

Key Stage 3: 2003 Paper 2 Level 3-5

Tier & Question 8-5 4-6 5-7 6-8			on		Cala
-5 4	-6 5	5-7 6	-8		Coin
6 1	0	5		Correct response	Additional guidance
1 2	а	a	1m	Gives a correct explanation eg 2 \(\frac{2}{4} = \frac{1}{2} \) Two of the four coins are 10p so half of them are 10p 20p is \(\frac{1}{4} \), so is 1p, and \(\frac{1}{4} + \frac{1}{4} + \frac{1}{2} = 1 \) Each coin has \(\frac{1}{4} \) chance and \(\frac{1}{4} + \frac{1}{4} = \frac{1}{2} \)	✓ Minimally acceptable explanation eg • 2/4 • Two out of four • Two is half of four • Two are tens, two not ★ Incomplete explanation eg • It's 50/50 • There are two tens, a twenty and a 1p • There are two 10ps • Half the coins are 10ps • 20p is 1/4, so is 1p
1	b	b	1m	Identifies the values of the four coins as 20, 10, 2 and 1 and gives the probability $\frac{1}{4}$, or equivalent probability	! Values of coins identified but doubt expressed as to whether this is the only possible combination Condone * Probability stated without values of coins identified

Key Stage 3: 2003 Paper 1 Level 4-6

10 5		Correct response	Additional guidance
a a	2m	Indicates only the five points with positive integer coordinates whose sum is 6 eg	! Point(s) not indicated accurately Accept in parts (a) and (b) provided the pupil's intention is clear
	or	* * * * * * * * * * * * * * * * * * * *	! Additional points indicated that assume zero to be on the dice eg • (0, 6) and/or (6, 0) indicated If this is the only error, mark as 1, 0 ! Additional points with non-integer coordinates whose sum is 6 indicated eg •
	1m	Indicates at least four correct points with no incorrect points or Indicates all five correct points with not more than one incorrect point	If this is the only error, mark as 1, 0
ьь	2m	Indicates only the six points with positive integer coordinates such that $y = x$ eg	! Additional point indicated that assumes zero to be on the dice eg • (0, 0) indicated If this error has been penalised in part (a) condone If this is the only error and it has not been penalised in part (a), mark as 1, 0
	or 1m	Indicates at least five correct points with no incorrect points or Indicates all six correct points with not more than one incorrect point	! Additional points with non-integer coordinates such that y = x indicated eg . If this error has been penalised in part (a),
			condone If this is the only error and it has not been penalised in part (a), mark as 1, 0

Tier & Question			Thursday dies (south	
1-5 4-6 5-7 6	-8		Throwing dice (cont)	
0 5		Correct response	Additional guidance	
e e	1m	Completes the sentence to give a correct rule eg One less than the number on the red dice Red - 1 Needing 1 added to get the number on the red dice	✓ Minimally acceptable rule eg • 1 below the other dice • The number below the red dice ✓ Rule expressed algebraically eg • b = r - 1 • r - 1 ! Rule that does not use the given starting phrase Accept only if unambiguous eg, accept • Red = blue + 1 eg, do not accept • 1 more on the red ✓ Ambiguous rule eg • - 1 • 1 below • A number below the red dice • The number lower than the red dice • Followed by the number on the red dice ✓ Incomplete rule eg • Less than the number on the red dice ✓ Rule not generalised Do not accept rules only shown through particular numerical examples eg • 2 - 1 = 1, 3 - 2 = 1, 4 - 3 = 1 etc	

Key Stage 3: Paper 2 Level 4-6

Tier & Question						Cain
-5 4-	6 5	5-7	6-8			Coin
6 10	0	5			Correct response	Additional guidance
a a	1	a		1m	Gives a correct explanation eg • $\frac{2}{4} = \frac{1}{2}$ • Two of the four coins are 10p so half of them are 10p • 20p is $\frac{1}{4}$, so is 1p, and $\frac{1}{4} + \frac{1}{4} + \frac{1}{2} = 1$	✓ Minimally acceptable explanation eg • 2/4 • Two out of four • Two is half of four • Two are tens, two not
					■ Each coin has $\frac{1}{4}$ chance and $\frac{1}{4} + \frac{1}{4} = \frac{1}{2}$	 Incomplete explanation eg It's 50/50 There are two tens, a twenty and a 1p There are two 10ps Half the coins are 10ps 20p is ¹/₄, so is 1p
ь ь і	ь		1m	Identifies the values of the four coins as 20, 10, 2 and 1 and gives the probability $\frac{1}{4}$, or equivalent probability	! Values of coins identified but doubt expressed as to whether this is the only possible combination Condone	
				(U1)		× Probability stated without values of coins identified

Key Stage 3: 2004 Paper 1 Level 3-5

Tier & Question				Diagton	
4-6	5-7	6-8			Plasters
10	3			Correct response	Additional guidance
a	a		1m	1/35	! Answer given as a decimal or a percentage without a correct fraction shown Accept decimals within the following ranges or their percentage equivalents: part (a) 0.028 to 0.03 inclusive part (b) 0.45 to 0.46 inclusive part (c) 0.54 to 0.55 inclusive
ь	b		1m	16 35	! Words given alongside a correct probability Ignore eg, for part (a) accept • Unlikely, $\frac{1}{35}$
c	c		1m	19/35	
	4-6 10 a	4-6 5-7 10 3 a a	4-6 5-7 6-8 10 3 a a	4-6 5-7 6-8 10 3 a a 1m b b 1m	4-6 5-7 6-8 10 3

Key Stage 3: 2004 Paper 1 Level 4-6

Tier & Question					DIt
4-6	5-7	6-8			Plasters
10	3			Correct response	Additional guidance
а	a		1m	1/35	! Answer given as a decimal or a percentage without a correct fraction shown Accept decimals within the following range or their percentage equivalents: part (a) 0.028 to 0.03 inclusive part (b) 0.45 to 0.46 inclusive part (c) 0.54 to 0.55 inclusive ! Words given alongside a correct probabilit Ignore eg, for part (a) accept • Unlikely, \frac{1}{35}
b	ь		1m	16 35	
c	c		1m	19 35	
	4-6 10 a	4-6 5-7 10 3 a a	4-6 5-7 6-8 10 3 a a	4-6 5-7 6-8 10 3 a a 1m b b 1m	4-6 5-7 6-8 10 3

Key Stage 3: 2005 Paper 2 Level 3-5

7.

	Tier & Question		_	-			Counters
	4-6 12	-	6-8		Correct response	Additional guidance	
a	a	а		1m	$\frac{1}{3}$ or equivalent probability	! Value rounded Accept 0.33 or better, or the percentage equivalents	
Ь	ь	ь		1m	3		

Key Stage 3: 2005 Paper 2 Level 4-6

Tier	lier & Question					Counters
3-5	4-6	5-7	6-8			Counters
20	12	4			Correct response	Additional guidance
a	a	a		1m	$\frac{1}{3}$ or equivalent probability	! Value rounded Accept 0.33 or better, or the percentage equivalents
ь	ь	ь		1m	3	

Tier	& Q	uest	tion			Hands
-5	4-6	5-7	6-8			nanus
-	20	12	4		Correct response	Additional guidance
	a	а	a	1m	$\frac{7}{15}$ or equivalent probability	! Value rounded or truncated Accept 0.46() or 0.47 or the percentage equivalents Do not accept 0.5 unless a correct method or a more accurate value is seen
	b	ь	ь	1m	$\frac{1}{10}$ or equivalent probability	! Follow through Accept follow through from an incorrect total number of pupils seen in part (a), provided their total is not 4, 16 or 27 eg, from 14/29 for part (a) accept • 3/29
	c	c	c	1m	$\frac{2}{3}$ or equivalent probability	! Value rounded Accept 0.66() or 0.67 or the percentage equivalents

Tier &	Que	estic	n		Cninning
-5 4-	6 5	7 6	-8		Spinning
22	2 1	4	6	Correct response	Additional guidance
			2	0.15 or equivalent probability	 ★ For 2m, incorrect notation eg 0.1 ½ 0.1.5
			1	Shows or implies the intention to add the given probabilities, subtract the sum from 1 and then divide by 2, even if there are errors eg • $0.1 + 0.6 = 0.7$ • $\frac{1 - 0.7}{2}$ • $0.3 + 2$ • $\frac{1.5}{10}$	

Key Stage 3: 2006 Paper 2 Level 3-5

11.

Tier	8 0	ues	tion			Cattand
1-5	4-6	5-7	6-8			Cat food
18	9	1			Correct response	Additional guidance
a	а	a		1m	$\frac{1}{4}$ or equivalent probability	
Ь	ь	ь		1m	$\frac{1}{3}$ or equivalent probability	! Probability rounded Accept 0.33 or better, or percentage equivalents
c	c	c		1m	0.3 or equivalent probability	

Key Stage 3: 2006 Paper 2 Level 4-6

Tier	8 0	(uest	ion			Cat food
3-5	4-6	5-7	6-8			Cat 1000
18	9	1			Correct response	Additional guidance
a	a	a		1m	$\frac{1}{4}$ or equivalent probability	
ь	Ь	ь		1m	$\frac{1}{3}$ or equivalent probability	! Probability rounded Accept 0.33 or better, or percentage equivalents
c	c	c	T	1m	0.3 or equivalent probability	

Key Stage 3: 2007 Paper 1 Level 3-5

13.

Tier & Question				Sweets		
3-5	4-6	5-7	6-8			
18	11	3			Correct response	Additional guidance
a	a	a		1m	$\frac{1}{20}$ or equivalent probability	
b	ь	Ь		1m	Indicates green	✓ Unambiguous indication of colour eg • G

Key Stage 3: 2007 Paper 2 Level 3-5

14.

Tie	r & Q	uest	tion			Spinners
3-5	4-6	5-7	6-8			E.F. (1997)
21	14	5			Correct response	Additional guidance
a	a	a		1m	Indicates B	
ь	ь	ь		1m	Indicates A and D, in either order	_

Key Stage 3: 2007 Paper 1 Level 4-6

Tier & Question		d		Mary and a		10.00		10		d		d		d on a		d				Sweets
-0.00	1000	3	6-8		Correct response	Additional guidance														
a	a	a		1m	$\frac{1}{20}$ or equivalent probability															
ь	b	b		1m	Indicates green	✓ Unambiguous indication of colour eg • G														

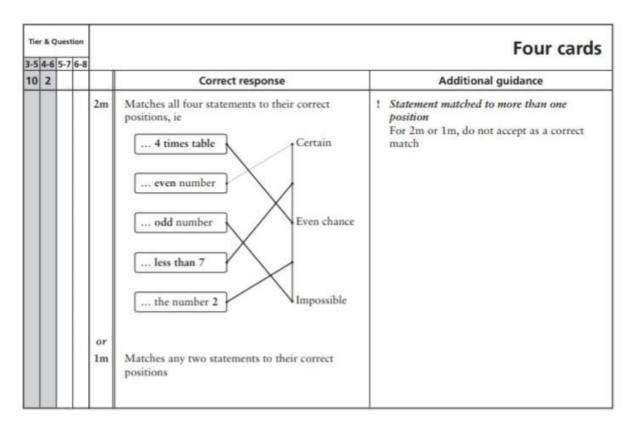
4-6 5		6-8					Counter probabilitie
19 1	_			(orrect respons	se	Additional guidance
a	a	a	2m	Completes the table with the three correct values in the correct positions, ie		✓ Equivalent probabilities	
				Colour of counters	Number of counters	Probability	× Incorrect notation eg
				Red	6	<u>2</u> 5	• 1/2.5
	ı			Blue	3	<u>1</u> 5	
				Green	6	2/5	
			1 m	Cinas as large		in the second	
ь	b	b	1m U1 1m	Gives at least on position Indicates that the		econtribute contribute of a contribute	

Key Stage 3: 2007 Paper 2 Level 4-6

Tier & Question		100401	100401	00000		22.432			Spinners
_	-		6-8	_					
21	14	5			Correct response	Additional guidance			
a	a	a	0:5	1m	Indicates B				
ь	b	Ь		1m	Indicates A and D, in either order				

Tier & C	Quest	ion			Vo
5 4-6	_	$\overline{}$,		
30	21	10		Correct response	Additional guidance
		a	2m	0.61 or equivalent probability	
			or		
			1m	Shows the digits 61	
				or	
				Shows the value 0.39 or equivalent probability	
				or	
				Shows or implies a complete correct method with not more than one computational error eg $ = 1 - (0.08 + 0.13 + 0.07 + 0.08 + 0.03) $ $ = 0.08 + 0.13 + 0.07 + 0.08 + 0.03 = 0.38 $ $ (error) $ $ 1 - 0.38 = 0.62 $	
		b	2m	0.000936 or 9.36×10^{-4} , or equivalent probability	× For 2m, 9.36 ⁻⁰⁴
			or		
			1m	Shows the digits 936	
				or	
				Shows or implies a complete correct method with not more than one computational error eg 0.13 × 0.08 × 0.09 9.4 × 10 ⁻⁴	

Key Stage 3: 2008 Paper 2 Level 3-5



Key Stage 3: 2008 Paper 2 Level 4-6

10 2	6-8	Correct response	Additional guidance
	2m or 1m	Matches all four statements to their correct positions, ie 4 times table even number odd number Even chance less than 7 the number 2 Impossible	Statement matched to more than one position For 2m or 1m, do not accept as a correct match

5 4-6 5-7				Counters in a ba
24 15	_		Correct response	Additional guidance
		2m	Completes the sentence correctly with three positive integers r , w then y , such that $w = 2r$ and $y < r$ eg 2, 4 then 1 3, 6 then 1 or 2 4, 8 then 1, 2 or 3	
		or		
		1m	Completes the sentence with three integers r , w then y , such that $w = 2r$ and $y = 0$ eg 2, 4 then 0 3, 6 then 0 or Completes the sentence with three values r , w then y between zero and one, such that $r > \frac{1}{4}$, $w = 2r$ and $r + w + y = 1$ eg 2, $\frac{4}{7}$ then $\frac{1}{7}$ 0.3, 0.6 then 0.1	x For 1m, values for r or w negative or zero eg -1, -2 then 0 0, 0 then 0

Key Stage 3: 2009 Paper 1 Level 3-5

22.

1.5	4-4	5-7 6-1			T-shirts
8	11	2	Mark	Correct response	Additional guidance
a	a	a	1m	½ or equivalent probability	
b	Ь	b	1m	² / ₃ or equivalent probability	! Value rounded Accept 0.66() or 0.67 or the percentage equivalents
c	c	c	1m	$\frac{1}{3}$ or equivalent probability	! Value rounded Accept 0.33() or the percentage equivalent

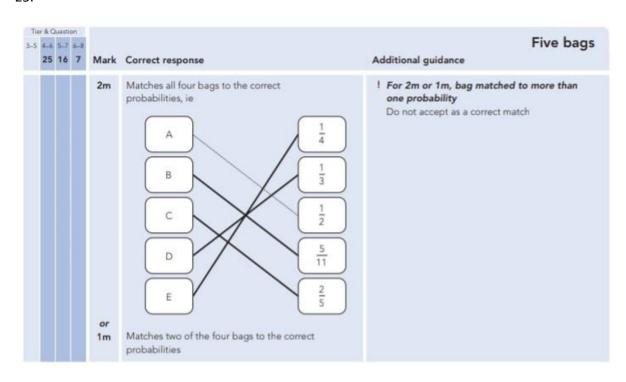
Key Stage 3: 2009 Paper 2 Level 3-5

Tier & Question 3-5 4-6 5-7 6-8 5 Mark	Correct response	Additional guidance	Spinner
2m or 1m	Makes all four correct decisions, ie True False V	✓ Unambiguous indication eg • ✓ for True, ➤ for False	

Key Stage 3: 2009 Paper 1 Level 4-6

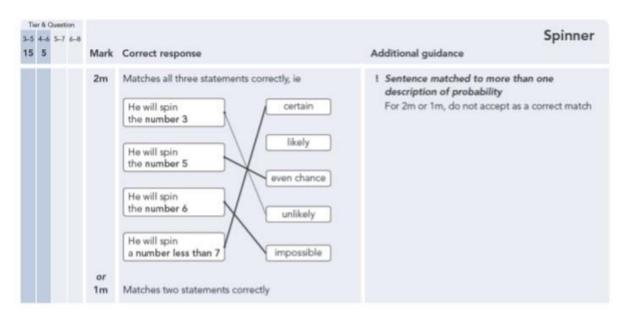
	Ter & Question 5 4-8 5-7 6-8				T-shirts
18	11	2	Mark	Correct response	Additional guidance
a	a	a	1m	1/5 or equivalent probability	
b	Ь	b	1m	² / ₃ or equivalent probability	! Value rounded Accept 0.66() or 0.67 or the percentage equivalents
c	c	с	1m	$\frac{1}{3}$ or equivalent probability	! Value rounded Accept 0.33() or the percentage equivalent

Key Stage 3: 2009 Paper 2 Level 4-6



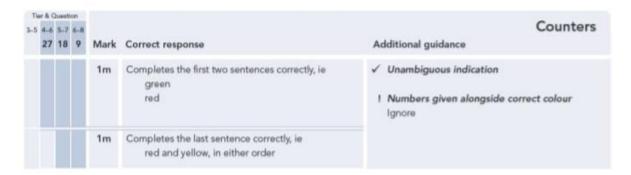
Key Stage 3: 2010 Paper 2 Level 3-5

26.

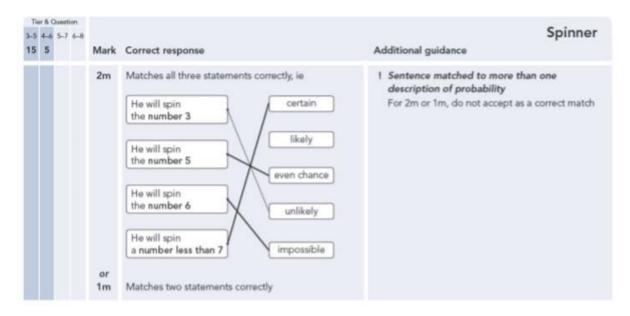


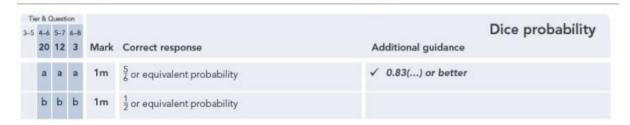
Key Stage 3: 2010 Paper 1 Level 4-6

27.



Key Stage 3: 2010 Paper 2 Level 4-6





Key Stage 3: 2011 Paper 1 Level 4-6

ier & Question			
4-6 5-7 11 2	Mark	Correct response	Additional guidance
11 2	Mark 2m	Correct response States or implies that the probabilities for A and C are $\frac{1}{6}$ and that the probability for B is different or unknown eg • Dice A: The probability is $\frac{1}{6}$ Dice B: You would need to do an experiment Dice C: It's the same as A • Dice A: It looks like probability is $\frac{1}{6}$ assuming they are fair dice Dice B: I would guess that the probability is more Dice C: It's $\frac{1}{6}$ if it is fair	Additional guidance ✓ Explanations do not refer to 'probability' eg, accept • Dice A: ½ Dice B: Don't know Dice C: ½ ✓ Probability for B quantified Condone eg, accept • Dice A: ½ Dice B: ⅓ Dice B: ⅓ Dice B: ⅓
	or 1m	States or implies that the probabilities for A and C are $\frac{1}{6}$ and does not comment on Dice B eg • Dice A: The probability is $\frac{1}{6}$ Dice B: Dice C: It's the same as A or States or implies that the probabilities for A and C are the same and the probability for B is different or unknown eg • Dice A: The probability is the same as C Dice B: You can't be sure Dice C: It's the same as A	Dice C: 1/6 X Probability incorrectly expressed Do not accept for 2m ! Probability incorrectly expressed For 1m condone provided equality is implied eg, accept • Dice A: The probability is 1 in 6 Dice B: You can't be sure Dice C: It's the same as A ! Likelihood expressed in words For 1m, accept as implying equality eg, accept • Dice A: It's unlikely Dice B: Likely Dice C: It's unlikely

Tier & Question			140	
4-6 5-7 18 9	Mark	Correct response	Win or lose Additional guidance	
	1m	Indicates Win and gives a correct explanation eg • $\frac{7}{12} > \frac{1}{2}$ • The numerator is more than half of the denominator • Six out of 12 is half, and this is more • 6 is half of 12 and $7 > 6$ • The probability of losing is $\frac{5}{12}$ therefore he is more likely to win	 ✓ Minimally acceptable explanation eg Half of 12 is 6 7 is over half way It's over half 7 is more than half More than a half chance Because 7 is only 5 away from 12 7 > 6 7 > 5 Losing is 5/12 An even chance is 6/12 The number at the top is lower than at the bottom 7 is 5 away from 12 7 is close to 12 It is over 6 He has more than half % probability to win 	

4-6	5-7			Coins and probability
25	16	Mark	Correct response	Additional guidance
		2m or 1m	Indicates Both equally likely and gives a correct explanation eg • Anna has 20p, 10p Her probability is $\frac{1}{2}$ Tom has 10p, 10p, 5p, 5p His probability is $\frac{2}{4} = \frac{1}{2}$ • Tom has two 10p coins and two other coins Anna has one 10p coin and one other Both have a half chance of choosing a 10p coin • For Tom the ratio of 10p coins to other coins is $2:2=1:1$ For Anna the ratio is also $1:1$ • For Tom, the ratio of total coins to 10p coins is $4:2$ For Anna, the ratio of total coins to 10p coins is $2:1$ $4:2=2:1$ Incorrect or no box ticked but gives a correct explanation	 ✓ Minimally acceptable explanation eg 20, 10 and 10, 10, 5, 5 1 in 2, 2 out of 4 (condone notation given context) Tom 2 × 10p Anna 1 × 10p 1 2 Anna = 1:1 He 4:2 She 2:1 For 2m, incomplete or incorrect explanation eg Both half She has 20 and 10 He has 10, 10, 20 (error), 5 Both half
			or For both Torn and Anna, gives the correct coins eg • Anna has 20p, 10p Tom has 10p, 10p, 5p, 5p or For Anna or for Tom, gives the correct probability and the correct number of 10p coins eg • Tom 10, 10, 5, 5 1/2 • Tom has 2 × 10p coins and 2 other coins	 ✓ Minimally acceptable explanation eg Anna = 20, 10 Tom = 10, 10, 5, 5 ✓ Minimally acceptable explanation eg Tom has 2 × 10p Half Anna has one 10p 0.5
			Half chance Anna has one 10p coin and 1 other coin Probability = 0.5 or Gives the correct probability or the correct ratio of 10p coins to other coins and indicates that this applies to both Tom and Anna eg Both have a half chance of choosing a 10p coin The ratio of 10p coins to other coins is 1:1 (with 'both equally likely' ticked)	 ✓ Minimally acceptable explanation eg Half (with 'both equally likely' ticked) Both 1:1

Key Stage 3: 2011 Paper 2 Level 4-6

Tier & C				C-11-
4-6	5-7		Correct response	Spinning Additional guidance
а	a	1m	С	! Spinners identified using probabilities
b	Ь	1m	В	$\frac{1}{3}$ for part (a) and $\frac{1}{4}$ for part (b) Mark as 0, 1
c	c	1m	Shows or implies that 4 of the 8 numbers are 2 eg	The only sectors labelled are 2 eg

	Duestion			144
4-6 24	5-7	Mark	Correct response	Word game Additional guidance
a	a	1m	Gives a correct probability eg • 70/100 • 0.29 • 29%	Probability See general guidance on page 16
b	ь	2m or 1m	Gives the values 8, 8 and 10 in the correct order 26 seen or Shows or implies + 13 eg • 104 + 13 • + 13 seen • Answer 32, 32, 40	! 8 seen Do not accept for 1m unless + 13 is implied x 13 seen without the operation